

(i) Printed Pages : 7]

Roll No.

(ii) Questions : 8]

Sub. Code :

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Exam. Code :

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**B.A./B.Sc. (General) 2nd Semester
Examination**

1047

MATHEMATICS

Paper : I (Solid Geometry)

Time : 3 Hours]

[Max. Marks : 30

Note :- Attempt *five* questions, selecting at least *two* questions from each Section.

Section-I

1. (a) Shift the origin to a suitable point so that the equation

$$2x^2 + 3y^2 + z^2 + xy + zx - x - 10y - 4z + 22 = 0$$

is transformed into an equation in which the first degree terms are absent.

- (b) If $\langle l_1, m_1, n_1 \rangle$ and $\langle l_2, m_2, n_2 \rangle$ be the direction cosines of two lines inclined at an angle θ , show that the direction - cosines of the direction bisecting them are :

$$\left\langle \left(\frac{l_1 + l_2}{2} \right) \sec \frac{\theta}{2}, \left(\frac{m_1 + m_2}{2} \right) \sec \frac{\theta}{2}, \left(\frac{n_1 + n_2}{2} \right) \sec \frac{\theta}{2} \right\rangle$$

3,3

2. (a) Find the equation of the sphere circumscribing the tetrahedron whose faces are $x = 0$, $y = 0$,

$$z = 0 \text{ and } \frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1.$$

- (b) Find the locus of the centres of the spheres passing through the fixed point $(0, 2, 0)$ and touching the plane $y = 0$.
- 3,3

3. (a) Prove that every sphere through the circle

$$x^2 + y^2 - 2ax + r^2 = 0, z = 0 \text{ cuts orthogonally}$$

every sphere through the circle $x^2 + z^2 = r^2,$

$$y = 0.$$

(b) Find the equation of a sphere which belongs to

the coaxial system whose limiting points are

(1, 2, 0), (2, 2, 0) and which passes through

the point (3, -1, 0).

3,3

4. (a) Find the equation of the right circular cylinder

described on the circle through the points

(2, 2, 0), (0, 2, 0) (0, 0, 2) as the guiding

circle.

- (b) Find the equation of the cylinder whose generators are parallel to the line

$$\frac{x-4}{3} = \frac{y}{5} = \frac{z-3}{-4} \text{ and whose guiding curve is}$$

$$\text{the hyperbola } 4x^2 - 3y^2 = 5, z = 2. \quad 3,3$$

Section-II

5. (a) The section of a cone whose vertex is P and

$$\text{guiding curve is the ellipse } \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1,$$

$z = 0$ by the plane $x = 0$ is a rectangular

hyperbola. Show that locus of P is

$$\frac{x^2}{a^2} + \frac{y^2 + z^2}{b^2} = 1.$$

- (b) Find the equation of cone with vertex (5, 4, 3)

$$\text{and guiding curve } 3x^2 + 2y^2 = 6, y + z = 0. \quad 3,3$$

6. (a) Show that the plane $6x + 3y - 2z = 0$ cuts the cone $yz + zx + xy = 0$ in perpendicular lines.

(b) Prove that the tangent planes to the cone $lyz + mzx + nxy = 0$ are at right angles to the generators of the cone

$$l^2x^2 + m^2y^2 + n^2z^2 - 2mnyz - 2nlzx$$

$$- 2lmxy = 0. \quad 3,3$$

7. (a) Show that $33x^2 + 13y^2 - 95z^2 - 144yz - 96zx - 48xy = 0$ represents a right circular cone whose axis is the line $3x = 2y = z$. Find its vertical angle.

(b) Show that the locus of the foot of the perpendicular from the centre of the ellipsoid

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1 \text{ to any of its tangent plane is :}$$

$$(x^2 + y^2 + z^2)^2 = a^2x^2 + b^2y^2 + c^2z^2 \quad 3,3$$

8. (a) Reduce the equation

$$11x^2 + 10y^2 + 6z^2 - 8yz + 4zx - 12xy + 72x - 72y + 36z + 150 = 0$$

to the standard form and show that it represents

an ellipsoid. Also find the equations of the

axes.

(b) If a right circular cone has three mutually perpendicular generators, then show that its

vertical angle is $\tan^{-1} \sqrt{2}$.

4,2

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MATHEMATICS

Paper : I (Solid Geometry)

Time : 3 Hours]

[Max. Marks : 80

Attempt five questions, selecting at least two questions from each Section.

Section-I

(a) Shift the origin to a suitable point so that the equation

$$2x^2 + 3y^2 + 2x + 3y + 1 = 0$$

$$-4x + 23 = 0$$

is transformed into an equation in which the

first degree terms are absent.