

(i) Printed Pages: 4] Roll No.

(ii) Questions : 8] Sub. Code :

0	1	4	6
---	---	---	---

Exam. Code :

0	0	0	2
---	---	---	---

**B.A./B.Sc. (General) 2nd Semester
Examination**

1047

MATHEMATICS

Paper : II Calculus-II

Time : 3 Hours]

[Max. Marks : 30

Note :- Attempt *five* questions in all selecting at least *two* questions from each Section.

Section-I

1. (i) Show that origin is the point of inflexion for the curve $y = x^{1/3}$.

(ii) Find the points of inflexion of the curve

$y = \frac{x^2 + 1}{x^2 - 1}$. Also find the interval where the

function is concave upwards and concave downwards.

2,4

2. (i) Find the nature and position of double points of the curve $y(y - 6) = x^2(x - 2)^3 - 9$.
- (ii) Trace the curve $x^{2/3} + y^{2/3} = a^{2/3}$. 3,3
3. (i) Find all asymptotes of the curve $x^3 - x^2y - xy^2 + y^3 + 2x^2 - 4y^2 + 2xy + x + y + 1 = 0$.
- (ii) Find the equation of the cubic curve which has the same asymptotes as the curve $x^3 - 6x^2y + 11xy^2 - 6y^3 + x + y + 1 = 0$ and which pass through the points $(0, 0)$, $(2, 0)$ and $(0, 2)$. 3,3
4. (i) Find the radius of curvature at the point $\left(\frac{3a}{2}, \frac{3a}{2}\right)$ on the curve $x^3 + y^3 = 3axy$.
- (ii) If C_x and C_y be chords of curvature parallel to axes of x and y respectively at any point of the curve $y = ae^{x/a}$, then prove that :

$$C_x^{1/2} + C_y^{1/2} = \frac{1}{2aC_x} \quad 3,3$$

Section-II

5. (i) Evaluate :

$$\int \frac{1}{\sqrt{\cosh 2x + \sinh 2x}} dx$$

(ii) If $I_n = \int_0^{\pi/2} x \sin^n x dx$, $n > 1$, $n \in \mathbb{N}$, prove

that $I_n = \left(\frac{n-1}{n} \right) I_{n-2} + n^{1/2}$. Hence evaluate

I_5 .

3,3

6. (i) If $I_{m,n} = \int \sin^m x \cos^n x dx$, prove that :

$$I_{m,n} = \frac{\sin^{m+1} x \cos^{n+1} x}{m+1} + \frac{m+n+2}{m+1} I_{m+2,n}$$

Hence evaluate $I_{-2,2}$.

(ii) Use Trapezoidal rule to approximate

$$\int_0^1 \frac{1}{1+x^2} dx \text{ by taking } n = 4. \text{ Also find the}$$

error.

3,3



7. (i) Evaluate :

$$\lim_{n \rightarrow \infty} \left[\frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} + \dots + \frac{1}{5n} \right]$$

(ii) Find the area bounded by the curves $y^2 = 8x$
and $x^2 + y^2 = 9$. 3,3

8. (i) Find the length of the arc of parabola $y^2 - 4y$
 $+ 2x = 0$ which lies in the first quadrant.

(ii) Find the volume of the solid formed by the
revolution about x-axis of the loop of the curve

$$y^2 (a + x) = x^2 (3a - x). \quad 3,3$$