7.	Printed Pages: 4		Roll No				
	d and		Sub. Code:	0	3	4	1
	Questions	:8	.Sub. Code:	0			

Exam. Code: 0 0 0 4

B.A./B.Sc. (General) 4th Semester

1046

## **MATHEMATICS**

Paper: III-Dynamics

Time Allowed: Three Hours] [Maximum Marks: 30

Note: Attempt five questions, selecting at least two questions from each Unit. Each question will carry 6 marks.

## **UNIT-I**

- I. (a) A bus is beginning to move with an acceleration 1 m/sec<sup>2</sup>.

  A man who is 40 m behind the bus starts running at 9 m/sec to catch the bus. After how many seconds will the man be able to catch the bus? Explain the double answer.

  If the man is 40½ m behind, will he be able to catch the bus?
  - (b) From the top of a tower 360 m high, a ball is projected downwards with an initial velocity of 10 m/sec. At the same instant another ball is projected upwards from the bottom with a velocity of 150 m/sec. Find the distance from the bottom of the tower of the point at which they pass each other. Also, prove that the sum of the speeds of the two balls at any instant is the same.

- II. (a) Two particles of masses m<sub>1</sub> and m<sub>2</sub> are connected by a light inextensible string, m<sub>2</sub> is placed on a smooth horizontal table.
   The string passes over a light smooth pulley at the edge of the table and m<sub>1</sub> is hanging freely. Find the tension in the string and pressure on the pulley.
  - (b) A balloon on mass m is rising with an acceleration f. Prove that the fraction of weight of balloon that must be detached in order to double its acceleration is  $\frac{mg}{2f + g}$  assuming that up thrust of air remains same.
- III. (a) The acceleration of a particle varies directly as time which has elapsed since its velocity was 10 m/sec. If it travels 168 m in 6 seconds, following this instant, find how far will it travel in next 4 seconds.
  - (b) A particle starts from rest under the action of its weight and a resistance equal to 'k v' per unit of mass, where k is a constant and v is velocity. Prove that:

(i) 
$$v = \frac{g}{k} (1 - e^{-kt})$$

(ii) 
$$s = \frac{g}{k^2} \left( kt + e^{-kt} - 1 \right)$$

(iii) 
$$ks + v + \frac{g}{k} \log \left| 1 - \frac{kv}{g} \right| = 0$$

where s is the distance travelled and t is the time in seconds.

- II. (a) Two particles of masses m<sub>1</sub> and m<sub>2</sub> are connected by a light inextensible string, m<sub>2</sub> is placed on a smooth horizontal table.
   The string passes over a light smooth pulley at the edge of the table and m<sub>1</sub> is hanging freely. Find the tension in the string and pressure on the pulley.
  - (b) A balloon on mass m is rising with an acceleration f. Prove that the fraction of weight of balloon that must be detached in order to double its acceleration is  $\frac{mg}{2f + g}$  assuming that up thrust of air remains same.
- III. (a) The acceleration of a particle varies directly as time which has elapsed since its velocity was 10 m/sec. If it travels 168 m in 6 seconds, following this instant, find how far will it travel in next 4 seconds.
  - (b) A particle starts from rest under the action of its weight and a resistance equal to 'k v' per unit of mass, where k is a constant and v is velocity. Prove that:

(i) 
$$v = \frac{g}{k} (1 - e^{-kt})$$

(ii) 
$$s = \frac{g}{k^2} (kt + e^{-kt} - 1)$$

(iii) 
$$ks + v + \frac{g}{k} \log \left| 1 - \frac{kv}{g} \right| = 0$$

where s is the distance travelled and t is the time in seconds.

- IV. (a) A particle moving with S.H.M. of period 12 seconds travels
  10 cm from position of rest in 2 seconds. Find amplitude,
  maximum velocity and velocity at the end of 2 seconds. 3
  - (b) An elastic string, to the middle of which a particle of mass m is attached, is stretched to twice its natural length and placed on a smooth horizontal table and its ends are then fixed. If the particle is displaced in the direction of string, then find period of oscillation.

## **UNIT-II**

- V. (a) Find expressions for acceleration along the tangent and normal of a particle moving along a plane curve.
  - (b) A shot is fired horizontally from the top of a tower with a velocity of 200 m/sec which hits the ground in 2 sec. What is the height of the tower? Also, find the distance from the foot of the tower where the shot strikes the ground.
- VI. (a) A particle moves down along the outside of a smooth vertical circle of radius r. If it starts from rest at depth  $\frac{r}{2}$  below the highest point, prove that it leaves the circle at distance  $\frac{r}{3}$  above the centre.
  - (b) A train moving at a rate of 50 km/hr is struck by stone moving with velocity of 40 km/hr making an angle of 60° with direction of train. Find the velocity with which the stone appears to a passenger in the train to strike the train. 3

- VII. (a) Prove that work done in stretching an elastic string is equal to the product of the extension and mean of initial and final tensions.
  - (b) If a particle moves under the action of a conservative system of forces, then prove that the sum of its kinetic and potential energies remains constant throughout the motion.
- VIII. (a) An elastic ball is dropped from a height h above the ground and at the same time a second equal ball is projected vertically upwards to meet the former. Show that the balls come to rest immediately after the impact if the second ball be projected with a velocity which would just carry it to a height h.

3

(b) A mass m after falling freely through distance a begins to raise a mass M (M > m) connected with it by means of an inextensible string over a smooth pulley. Show that M will return to its original position after time  $\frac{2m}{M-m}\sqrt{\frac{2a}{g}}$ . Also find the impulse of the jerk and the distance through which M rises.