

2071

B.A./B.Sc. (General) Second Semester
Statistics

Paper - 103: Probability Theory and Descriptive Statistics –II

Time allowed: 3 Hours

Max. Marks: 65

NOTE: Attempt five questions in all, including Question No. I which is compulsory and selecting two questions from each Unit. Simple non-programmable calculator is allowed. Statistical tables and log tables will be provided on request.

x-x-x

1. Answer the following:

- (i) Give any two applications of Geometric distribution.
- (ii) State the mean of Beta distribution of II kind and the condition for it to exist.
- (iii) State any three properties of Normal distribution.
- (iv) Define covariance between two random variables X and Y. What happens to the covariance when they are independent?
- (v) If the correlation between X and Y is 0.5, what is correlation between $5X$ and $-3Y$?
- (vi) State weak law of large numbers. (2,2,3,2,2,2)

UNIT-I

2. (a) Derive the mean and variance of Gamma distribution.
- (b) If a random variable X is a Poisson variable with $P(X=1) = P(X=2)$, find the variance of X.
- (c) Show that Binomial distribution tends to Poisson distribution under some conditions. (6,3,4)
3. (a) Derive the recurrence relation for the moments of Poisson distribution and explain its usefulness.
- (b) A random X has the following probability density function (pdf):
 $f(x) = 1/10, -5 < x < 5$ and $f(x) = 0$, otherwise. Find (i) $P(|X-1| < 3)$ and (ii) variance of X. Also find value of the constant 'k' for which $(X > k) = 2/5$. (6,7)
4. (a) Let X and Y follow Bivariate Normal distribution with $\mu_1=3=E(X)$, $\mu_2=1=E(Y)$, $\sigma_1^2=16=Var(X)$, $\sigma_2^2=25=Var(Y)$ and $\rho = 3/5=Corr(X,Y)$. State the conditional distribution of X given $Y = 4$ and its parameters.
- (b) If X is binomially distributed with parameters n and p, find the distribution of $Y=(n-X)$?
- (c) State the pdf of Exponential distribution and find its variance. (3,4,6)

(2)

5. (a). State Lindeberg-Levy central limit theorem and provide any of its two applications.
- (b) For a Binomial distribution with parameters (12,0.2), find $P[|X - E(X)| \geq 3\text{Var}(X)]$ and compare the result obtained by Chebyshev's inequality. (6,7)

UNIT-II

6. Consider the following bivariate data:

X: 3.31 2.41 2.11 3.01 2.13 2.41 2.10 2.41 2.09 3.00

Y: 4.09 3.84 2.97 3.22 3.96 2.76 3.42 3.38 3.28 2.93.

- (a) Find two regression equations describing the relationship between the two variables.
- (b) Compute coefficient of determination and give your interpretation.
- (c) Estimate X when Y = 2.00 and Y when X = 2.80. (8,3,2)
7. (a) Explain the use of partial and multiple correlation coefficients.
- (b) For a trivariate data set: $r_{12} = 0.60$, $r_{13} = -0.42$ and $r_{23} = -0.80$. Determine the multiple correlation coefficient $R_{1.23}$ and the partial correlation coefficient $r_{13.2}$ and interpret your results.
- (c) State the merits and demerits of rank correlation. (4,6,3)
8. (a) Explain the concept of consistency and independence of attributes. Also illustrate them with an example.
- (b) Calculate the coefficient of colligation from the following data:

$$(AB) = 35, (A\beta) = 15, (\alpha B) = 10, (\alpha\beta) = 15.$$

Also verify the relation between coefficient of association and coefficient of colligation for the given data. (8,5)

9. (a) For a bivariate data you are given that the variance of X is 9. The regression equations are $8X - 10Y + 66 = 0$ and $40X - 18Y - 214 = 0$. Find (i) average values of X and Y, (ii) correlation coefficient between two variables and (iii) standard deviation of Y.
- (b) Write down the properties of regression coefficients. (9,4)