

2071

M.A. (Economics) Second Semester
MAECO-203 : Quantitative Methods - II

Time allowed: 3 Hours

Max. Marks: 80

NOTE: Attempt five questions in all, including Question No. I which is compulsory and selecting one question from each Unit. Use of simple non-programmable calculator is allowed. Students may be provided statistical tables.

x-x-x

I. Attempt any ten of the following:-

a) Evaluate $\int \left(x^2 + 2x^3 + \frac{x^6}{7} \right) dx$

b) Evaluate $\int_2^3 (x^2 + 4x + 5) dx$

c) Define degree and order of a differential equation.

d) What do you mean by consumer's surplus?

e) Define order and degree of a difference equation.

f) Solve the following difference equation:-

$$y_{n+1} - 4 y_n = 0$$

g) What are the assumptions of linear programming?

h) Find the area to the left of $z = +1.58$

i) In relation to binomial distribution, a fair coin is tossed thrice. Find the probability of getting exactly 2 heads.

j) Write down the properties of an ideal estimator.

k) Consider a hypothetical population consisting three values: 1,2,3. List all possible samples of size 2 with replacement.

l) Define sampling and non-sampling errors.

m) Define statistic and parameter.

n) Define level of significance.

o) Write down application / uses of t-test.

(10x2)

P.T.O.

(2)

UNIT – I

II. a) Evaluate $\int \frac{1}{x^2 + 5x + 6} dx$

b) Evaluate $\int (x^3 + 5)^2 3x^2 dx$

c) The demand and supply laws for a commodity are

$$p_d = 18 - 2x - x^2 \text{ and}$$

$$p_s = 2x - 3$$

Find the consumer's surplus at equilibrium price.

(6,3,6)

III. a) Solve the following differential equation:-

$$\frac{dy}{dx} = e^{x-y} + x^2 \cdot e^{-y}$$

b) Solve $\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} - 5y = e^{3x}$

c) Obtain the demand function for a commodity for which elasticity of demand is constant ' α ' throughout.

(3x5)

UNIT – II

IV. a) Solve the following difference equation:-

$$y_x - 5y_{x-1} + 6y_{x-2} = 0, \text{ given } y_0 = 3, y_1 = 5$$

b) Solve $\Delta y_n = -7y_n$ by iterative method.

c) Solve the following equation:-

$$y_{x+2} - 7y_{x+1} + 12y_n = 0$$

(3x5)

V. a) Write down the applications of linear programming.

(3)

b) Solve graphically the following LPP:

Maximize, $Z = 4x + 5y$

Subject to constraints

$$2x + 3y \leq 12$$

$$2x + y \leq 8$$

$$\text{and } x, y \geq 0$$

(5,10)

UNIT – III

VI. a) An aptitude test for selecting officers in a bank was conducted on 1000 candidates, the average score is 42 and the standard deviation of scores is 24.

Assume normal distribution for the scores, find

- i) The numbers of candidates whose score exceed 60.
- ii) The number of candidates whose score lie between 30 and 66.

b) In a town 10 accidents take place in a period of 50 days. Assume that the number of accidents per day follows Poisson distribution, find the probability that there will be three or more accidents per day (Given: $e^{-0.2} = 0.8187$) (9,7)

VII. a) A population consists of five values:-

3,4,5,6, and 7. List all possible samples of size 3 without replacement from this population and calculate the mean, \bar{X} , of each sample. Verify that statistic (\bar{X}) is an unbiased estimate of the population mean

b) A random sample of 900 workers in a steel plant showed an average height of 67 inches with a standard deviation of 5 inches.

- i) Establish a 95% confidence interval estimate of the mean height of all the workers at the steel plant.
- ii) Establish a 99% confidence interval estimate of the mean height of all the workers at the steel plant. (8,7)

P.T.O.

(4)

UNIT – IV

- VIII. a) The mean of two large samples of sizes 1000 and 2000 are 168.75 cms and 170 cms respectively. Can the samples be regarded as drawn from a population with some mean and standard deviation of 6.25 cms at 5% level of significance?

b) 10 persons were appointed in a clerical position in an office. Their performance was noted giving a test and marks were recorded out of 50. They were given 6 months training and again they were given a test and marks were recorded out of 50.

Employees	A	B	C	D	E	F	G	H	I	J
Before Training	25	20	35	15	42	28	26	44	35	48
After Training	26	20	34	13	43	40	29	41	36	46

By applying the t-test, can it be concluded that the employees have been benefitted by training. (Given for d.f. = 9, $t_{0.05} = 2.262$) (7,8)

- IX. a) The number of automobiles accidents per week in a certain city were as follow:-

12, 8, 20, 2, 14, 10, 15, 6, 9, 4

All these frequencies in agreement with the belief that accident's numbers were the same during these 10 week period. (for $v = 9$, $\chi^2_{0.05} = 16.92$)

- b) Two investigators study the income of group of persons by the method of sampling. Following results were obtained by them:-

Investigators	Poor	Middle-class	Well to do	Total
A	160	30	10	200
B	140	120	40	300
Total	300	150	50	500

show that the sampling technique of at least one of the investigator is suspected. (Given the value of $\chi^2_{0.05}$ for 2 d.f. = 5.991) (7,8)

$x - \bar{x} - \bar{x}$